

# Automatic Design of Aircraft Arrival Routes with Limited Turning Angle

Tobias Andersson Granberg, Tatiana Polishchuk, Valentin Polishchuk, Christiane Schmidt



## Introduction: Air transportation, SIDs + STARs

Grid-based IP formulation

Experimental Study: Arlanda Airport

Conclusion/Outlook





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At most airports predesigned standard routes for departure and arrival:



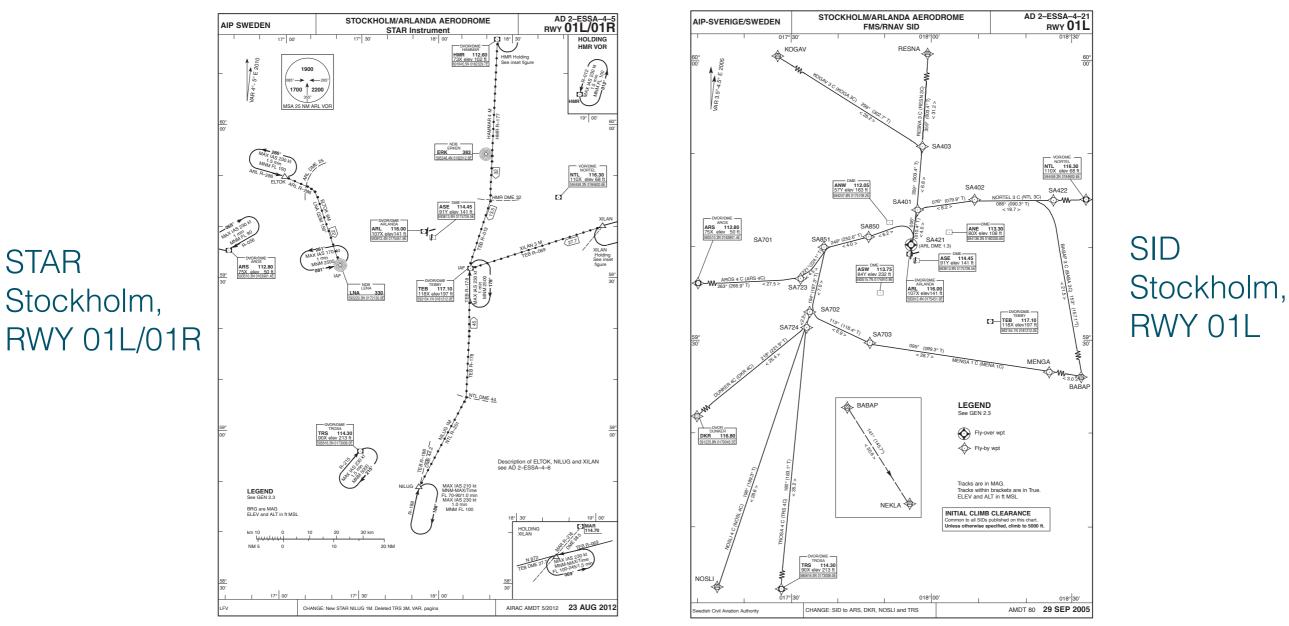
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5



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- No optimal routes for any specific criteria



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- here: mathematical programming framework for finding optimal STAR merge trees







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locations of the entry points to the TMA location and direction of the airport runway

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STAR–SID crossings far from the runway, where arriving and departing planes sufficiently separated **vertically** (difference of descend and climb slopes)



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Pareto frontier of multicriteria optimization problem: set of Pareto optimal solutions (cannot be improved with respect to one of the objectives without sacrificing on the other)







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- IP formulation is based on flow IP formulation for Steiner trees (Min Cost Flow Steiner arborescence)





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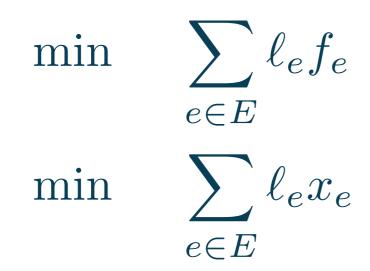


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$$\sum_{k:(k,i)\in E} f_{ki} - \sum_{j:(i,j)\in E} f_{ij} = \begin{cases} |\mathcal{P}| & i = r \\ -1 & i \in \mathcal{P} \\ 0 & i \in V \setminus \{\mathcal{P} \cup r\} \end{cases}$$

$$x_e \ge \frac{f_e}{N} \qquad \qquad \forall e \in E \\ f_e \ge 0 \qquad \qquad \forall e \in E \\ x_e \in \{0,1\} \qquad \qquad \forall e \in E \end{cases}$$







(2)











## Degree constraints:

$$\sum_{\substack{k:(k,i)\in E}} x_{ki} \leq 2 \quad \forall i \in V \setminus \{\mathcal{P} \cup r\}$$

$$\sum_{\substack{j:(i,j)\in E}} x_{ij} \leq 1 \quad \forall i \in V \setminus \{\mathcal{P} \cup r\}$$

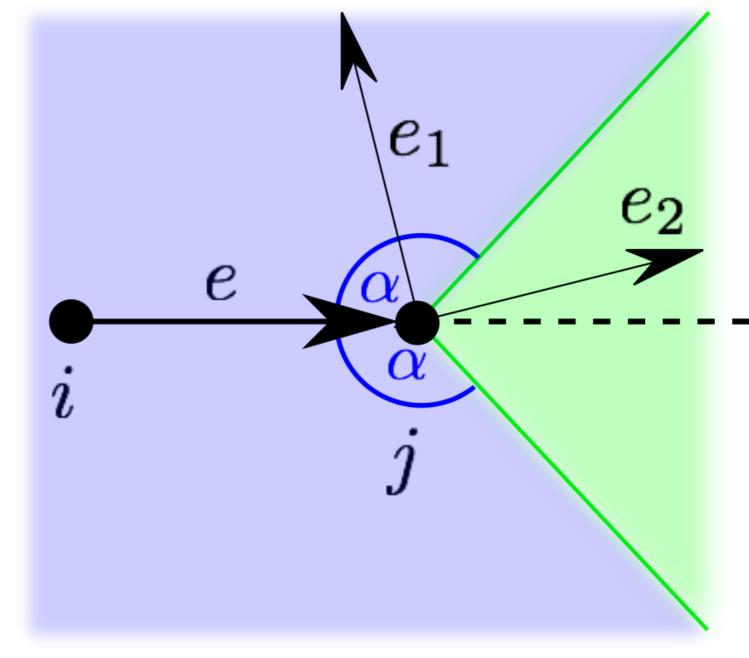
$$\sum_{\substack{k:(k,r)\in E}} x_{kr} = 1$$

$$\sum_{\substack{k:(k,i)\in E}} x_{rj} \leq 0$$

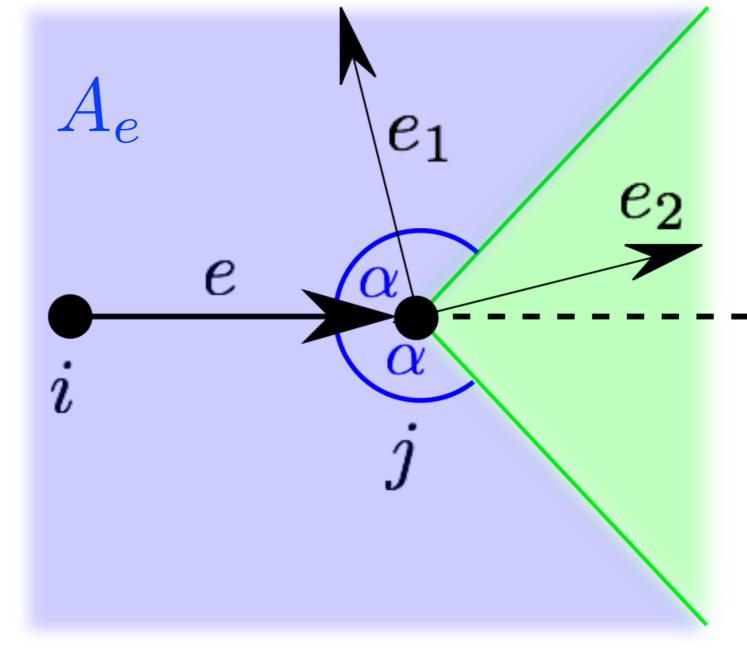
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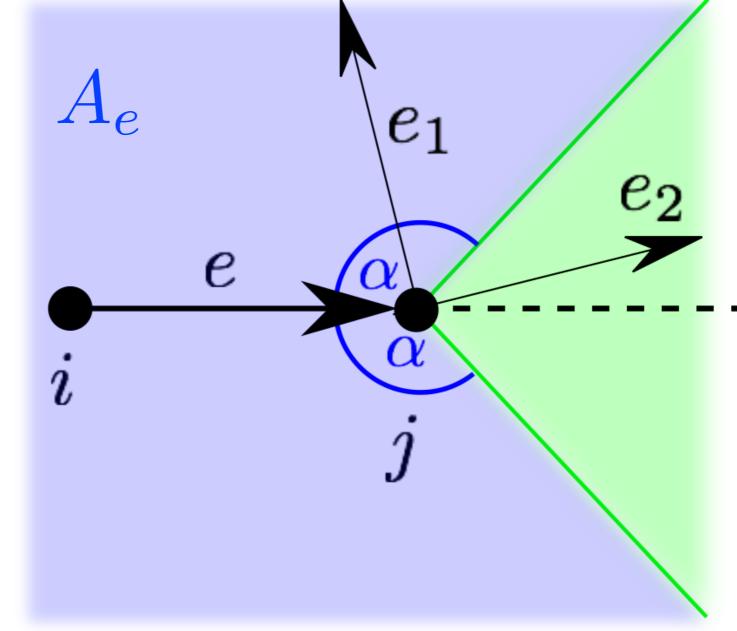






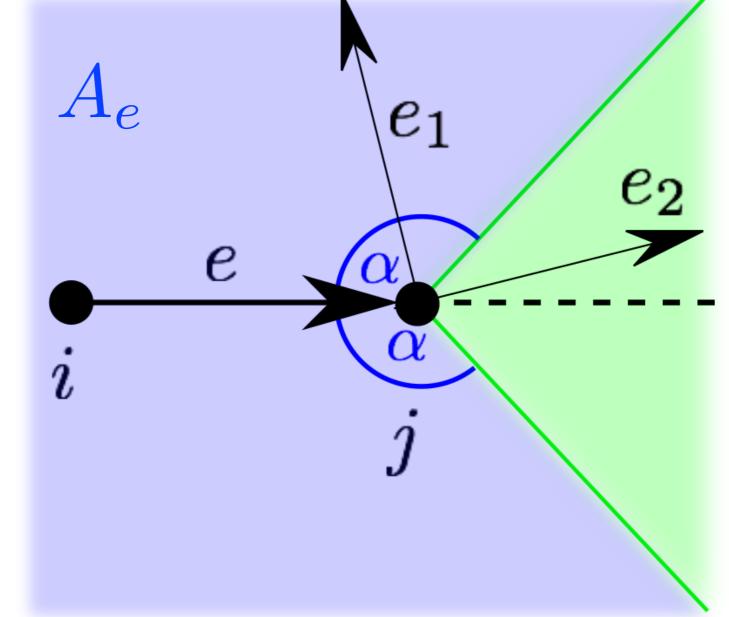






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$$a_e x_e + \sum_{f \in A_e} x_f \le a_e \ \forall e \in E$$

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# SID constraints: We disallow STAR edges to intersect SID edges within distance *d* from the runway.



### Experimental Study: Arlanda Airport





Stockholm TMA:Arlanda's runway 19L



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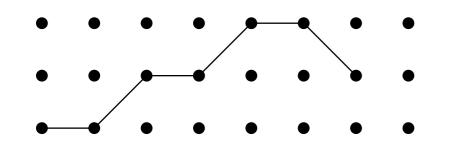
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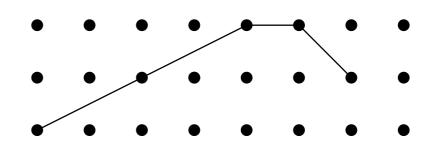
shortcuts by removing vertices as long as the turn angle constraint is not violated

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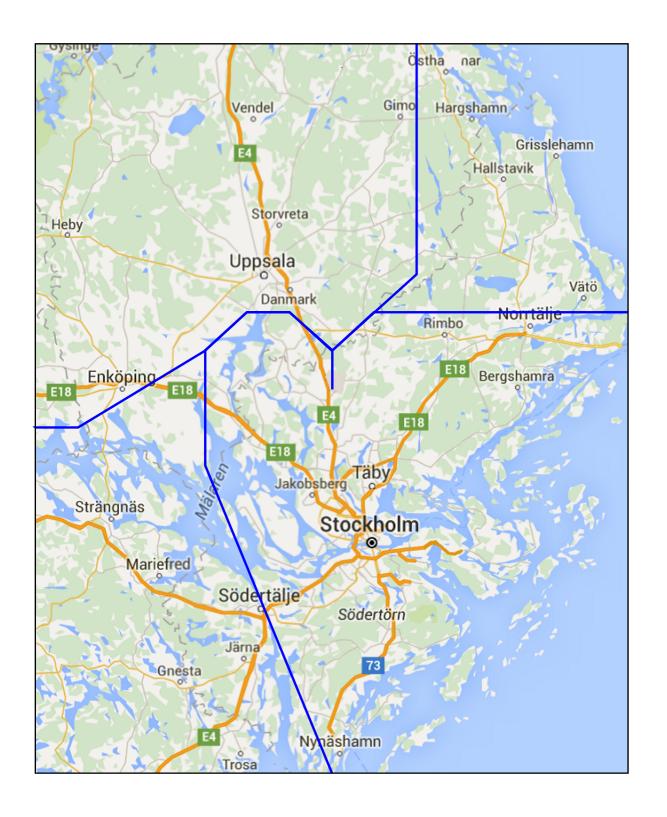
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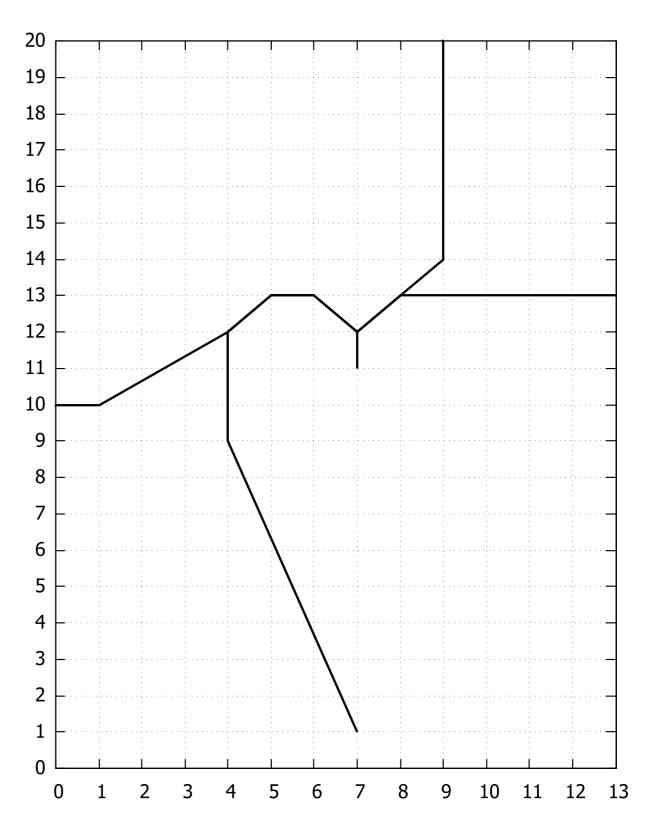
angle constraint is not violated





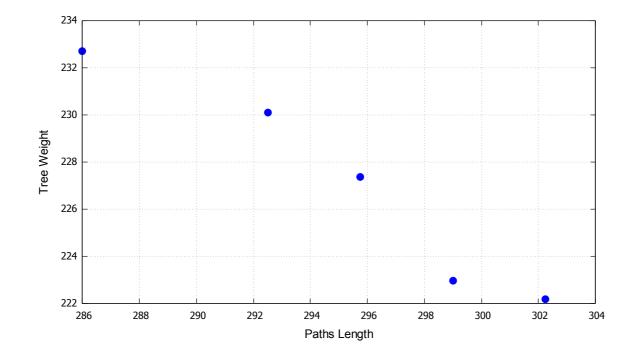




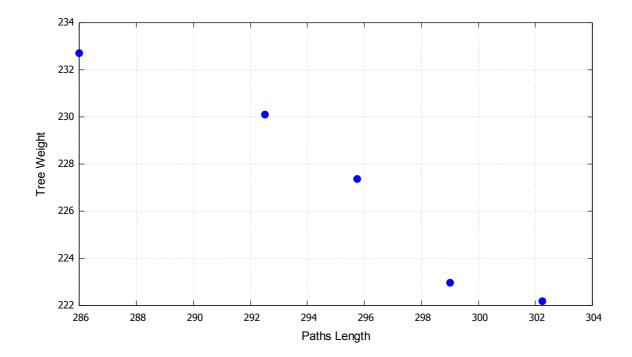




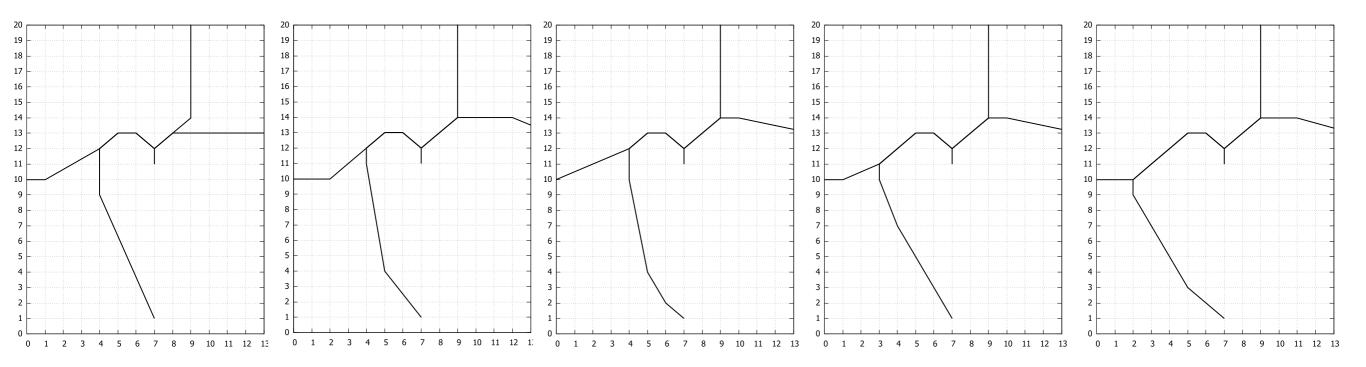
# Pareto frontier:



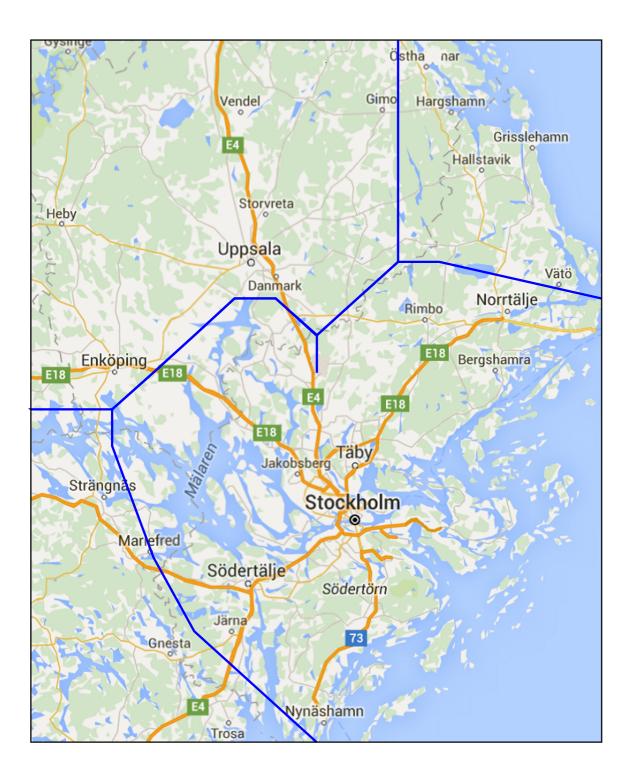


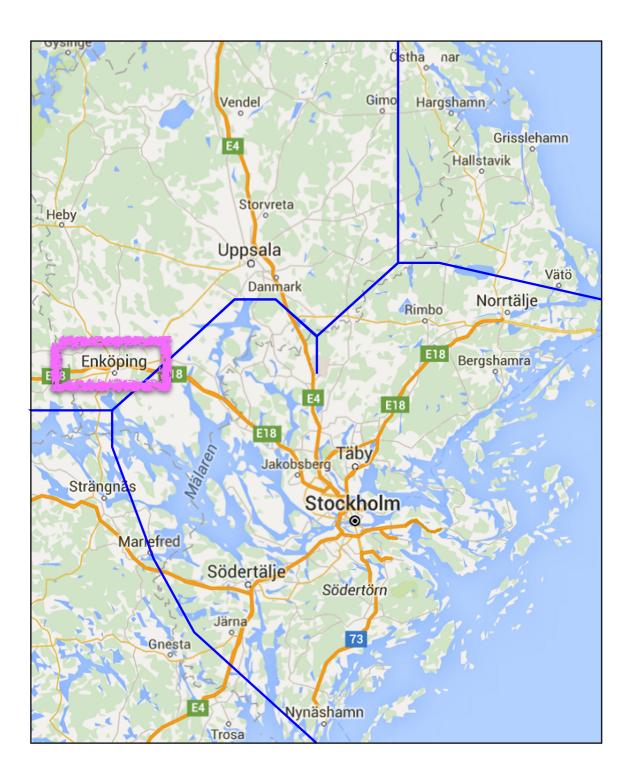


### Pareto optimal solutions:

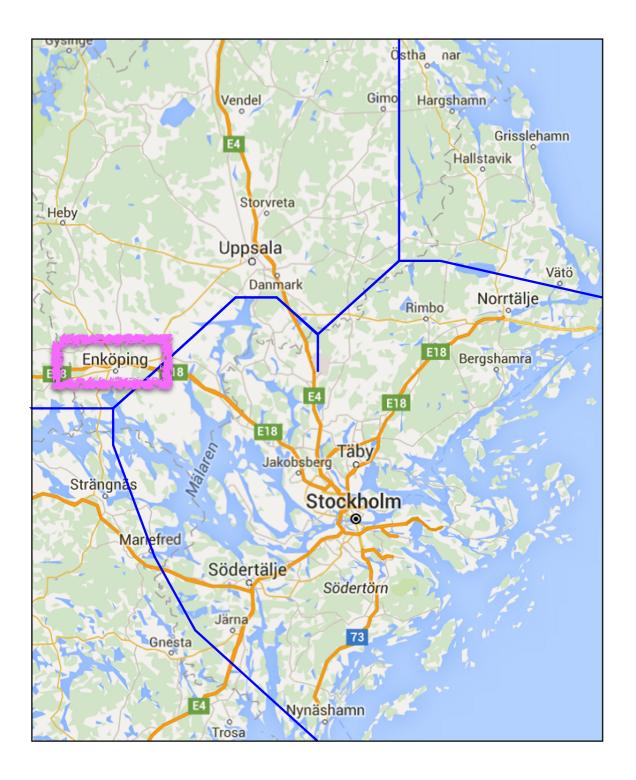


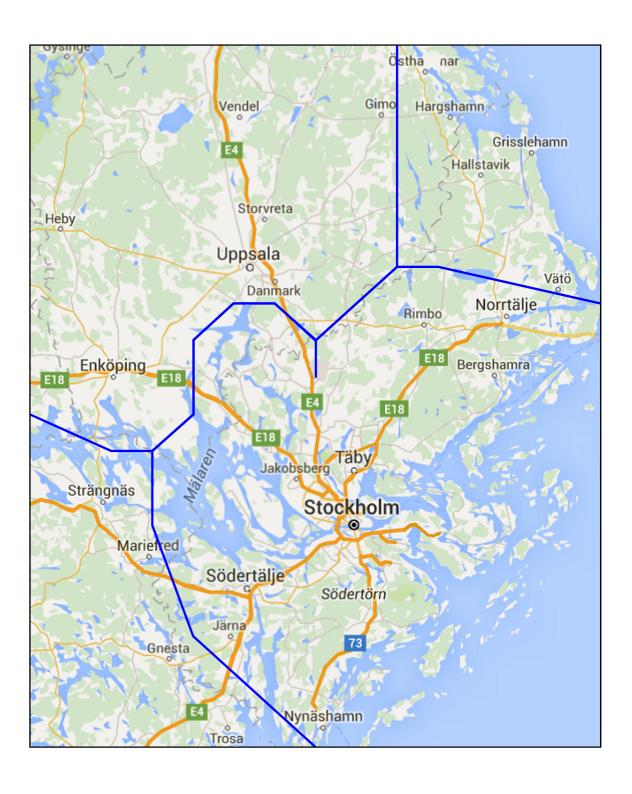












Increased Number of Entry Points:

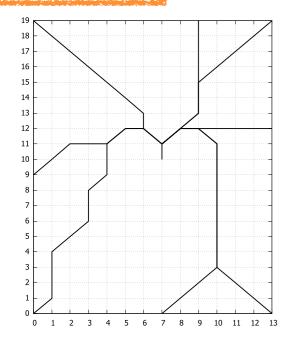


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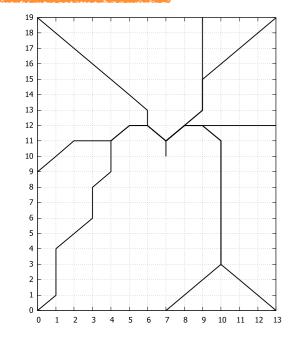


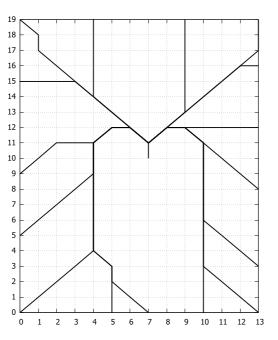


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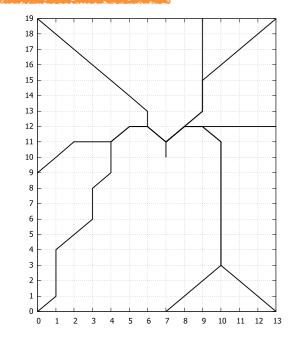


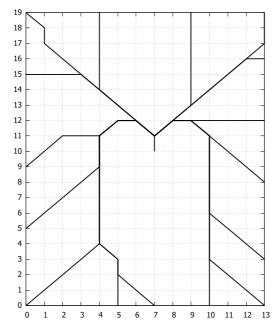


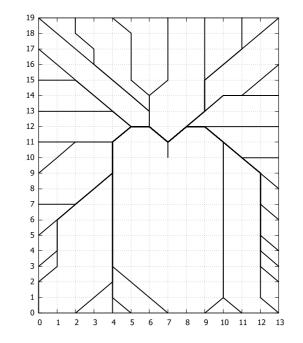




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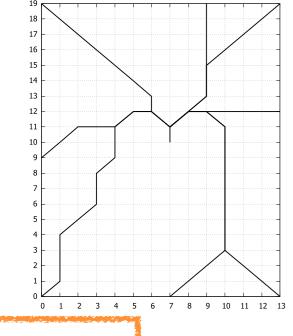


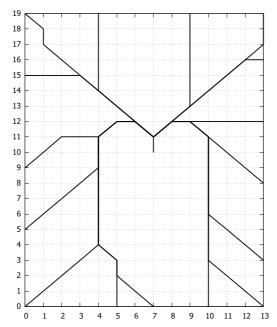


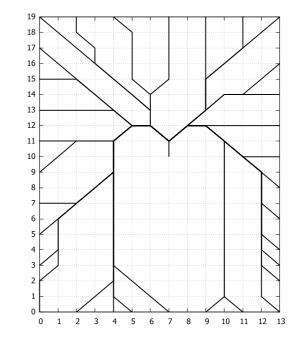


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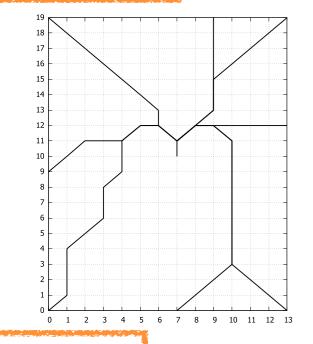


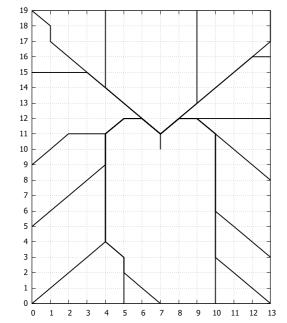
### tree weight

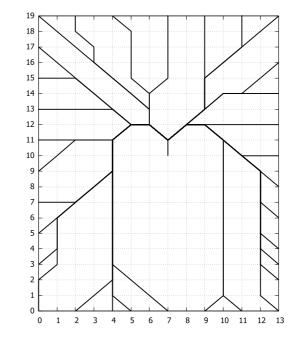


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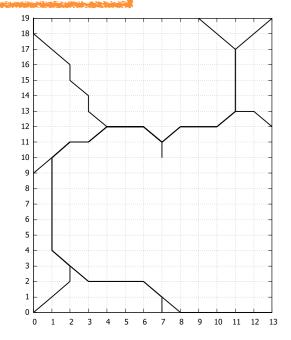
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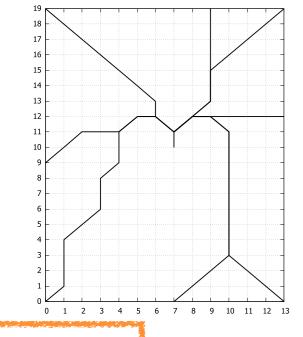
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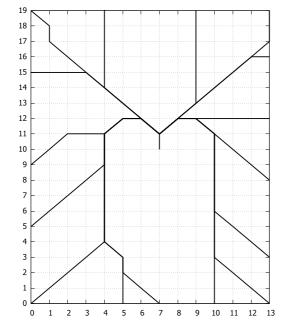


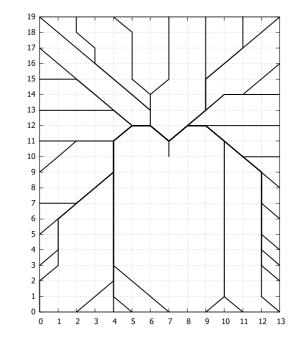


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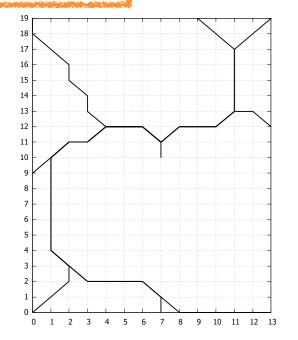
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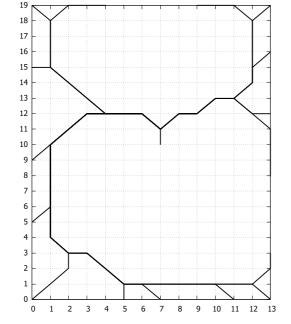






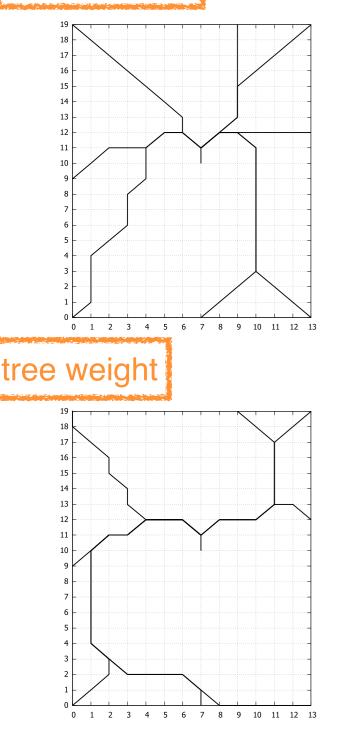
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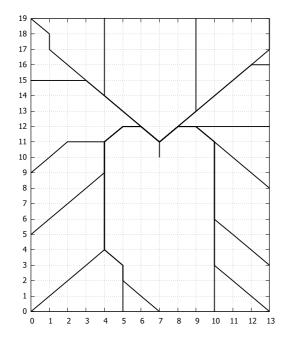


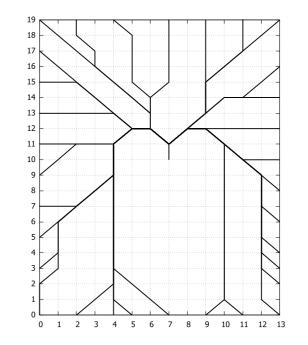


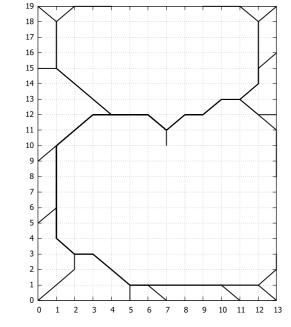


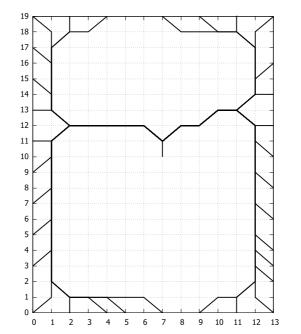
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17

16

15

14

13

12

11

10

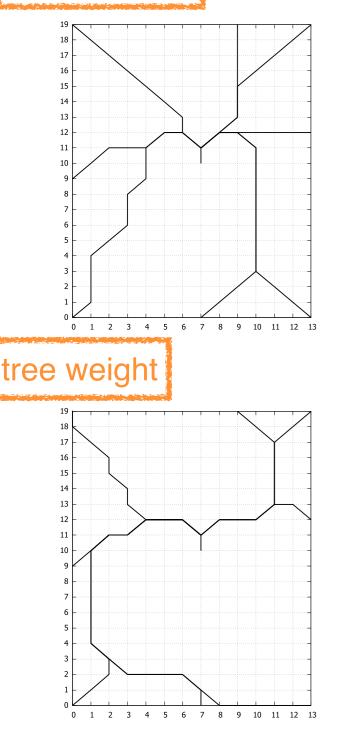
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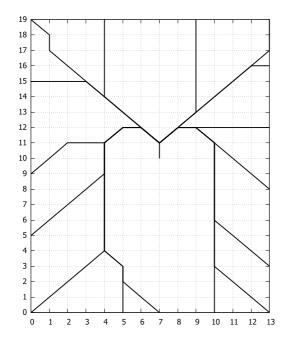
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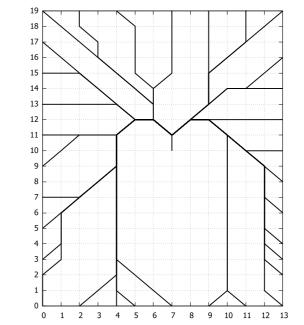
### Increased Number of Entry Points:

#### paths length

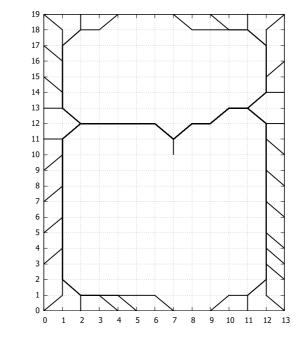




2 3 4 5 6 7 8 9 10 11 12 13



serve the airlines' request for short trajectories best

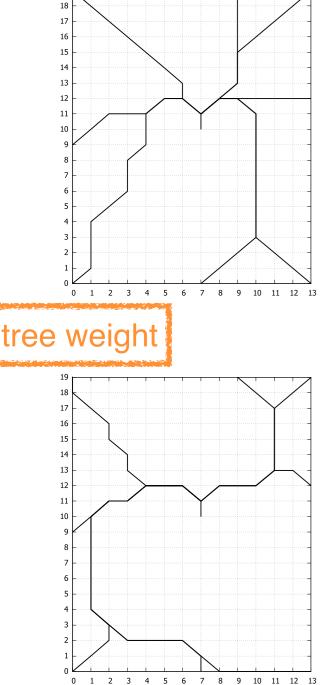


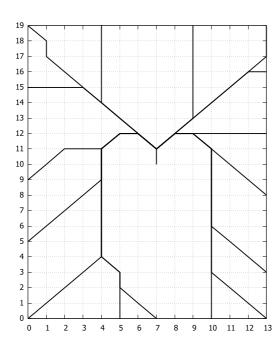
#### ATMOS, 25.08.2016

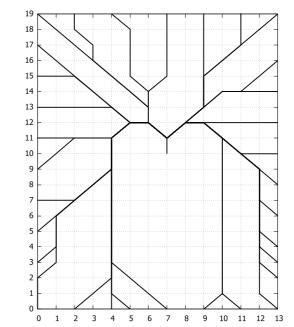


### Increased Number of Entry Points:

#### paths length



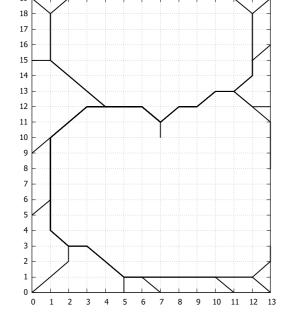


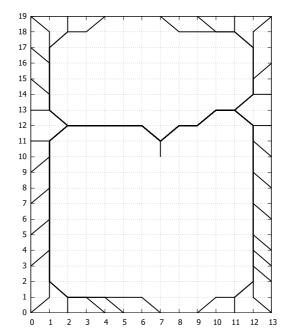


serve the airlines' request for short trajectories best

quite dense network of routes  $\rightarrow$ 





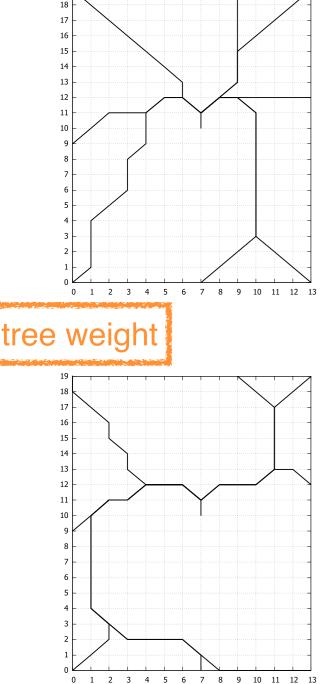


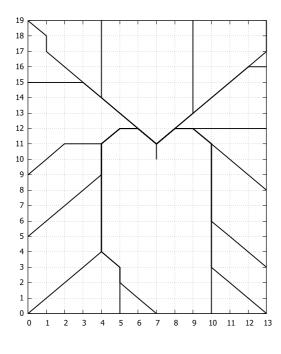
ATMOS, 25.08.2016

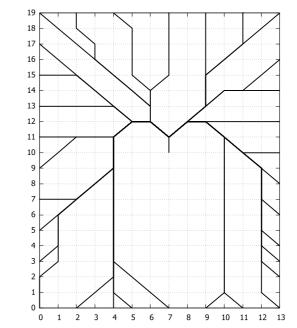


### Increased Number of Entry Points:

#### paths length

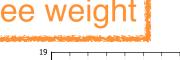


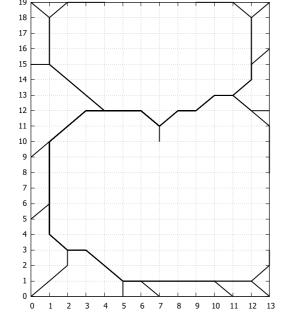


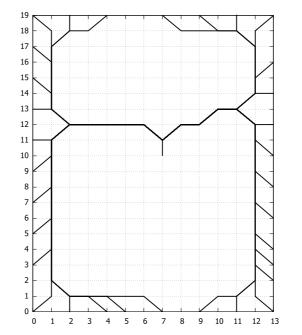


serve the airlines' request for short trajectories best

quite dense network of routes  $\rightarrow$ hard to control the traffic







17

15

14

13

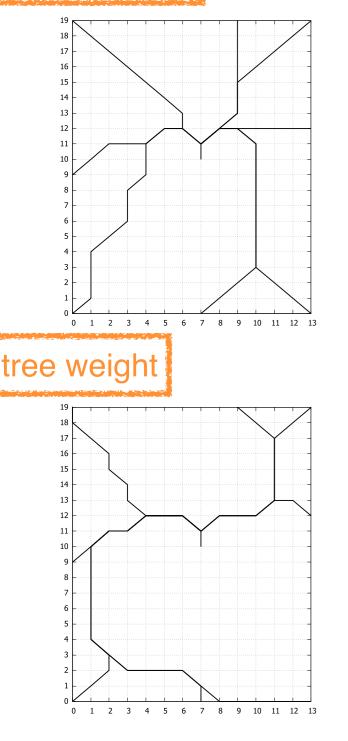
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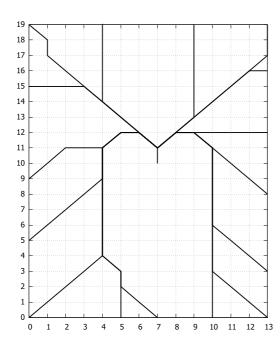
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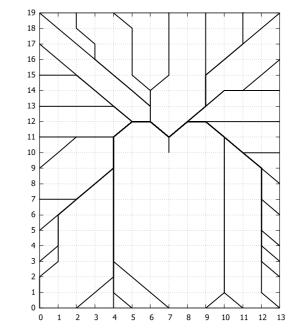
### Increased Number of Entry Points:

#### paths length





2 3 4 5 6 7 8



6

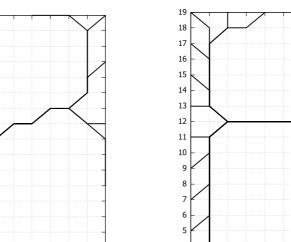
4 5

2 3

7 8 9 10 11 12 13

serve the airlines' request for short trajectories best

quite dense network of routes → hard to control the traffic



most merge points are located close to TMA boundary

10 11 12 13

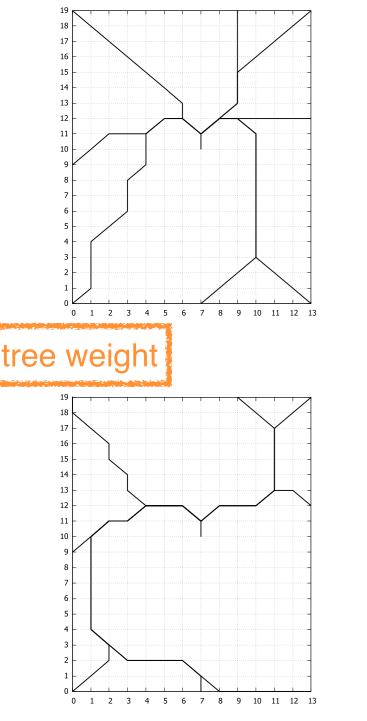
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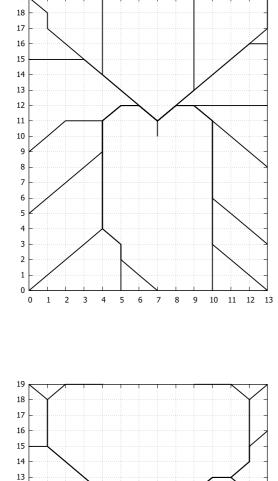
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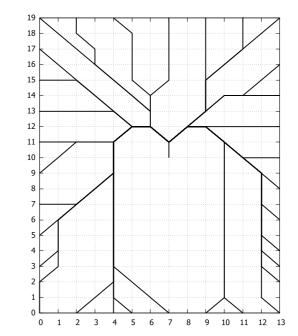


### Increased Number of Entry Points:

#### paths length

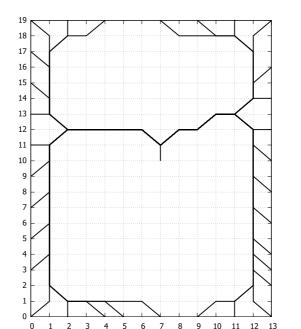






serve the airlines' request for short trajectories best

quite dense network of routes → hard to control the traffic



most merge points are located close to TMA boundary

### Helpful to use linear combination of these two functions

10 11 12 13

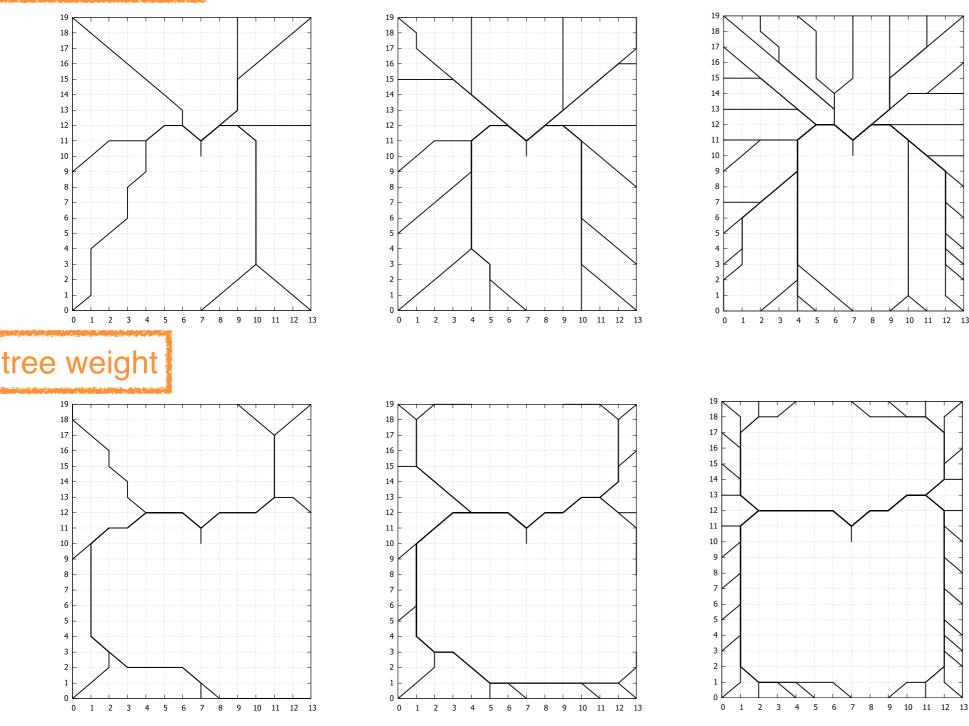
2 3 4 5

Automatic Design of Aircraft Arrival Routes with Limited Turning Angle



### Increased Number of Entry Points:

### paths length



### Helpful to use linear combination of these two functions

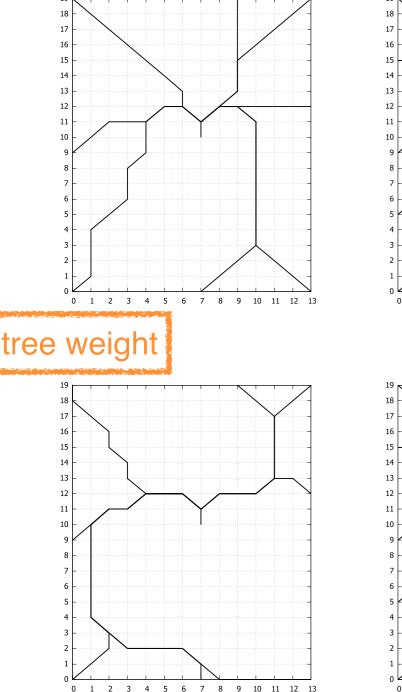
ATMOS, 25.08.2016

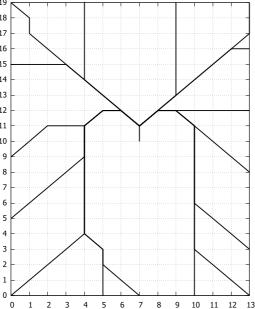
Automatic Design of Aircraft Arrival Routes with Limited Turning Angle

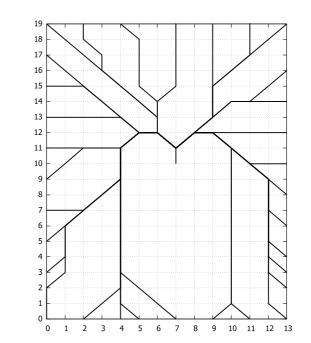


## Increased Number of Entry Points:

### paths length







8 9 10 11 12 13

Solutions for large number of entry points could be used to suggest the number and location of entry points for a design from scratch.

### Helpful to use linear combination of these two functions

10 11 12 13

2 3 4 5

6 7

Automatic Design of Aircraft Arrival Routes with Limited Turning Angle

15

14

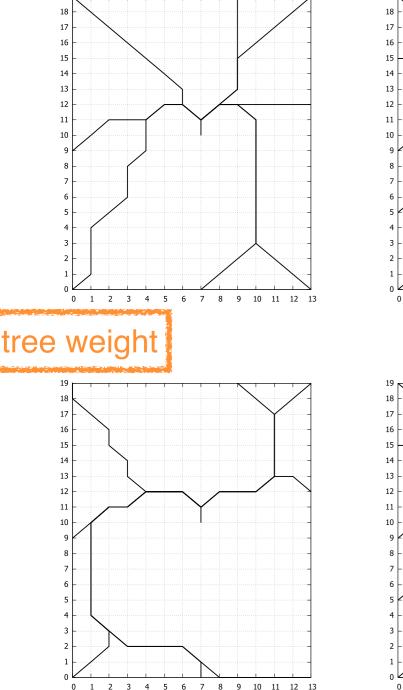
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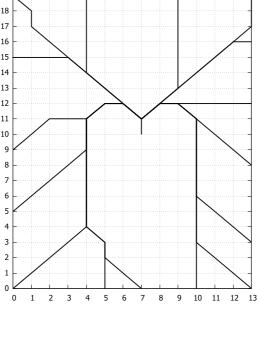
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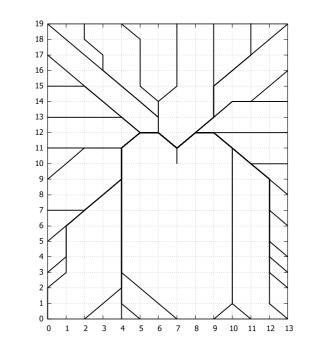


# Increased Number of Entry Points:

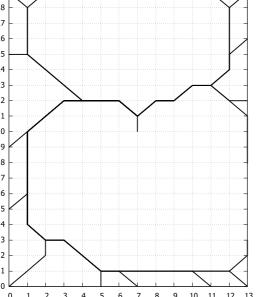
#### paths length

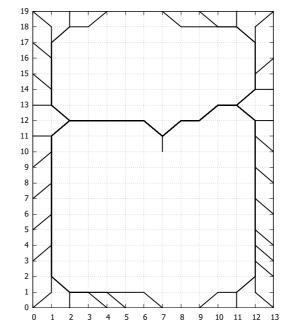






Solutions for large number of entry points could be used to suggest the number and location of entry points for a design from scratch.





2 entry points

### Helpful to use linear combination of these two functions

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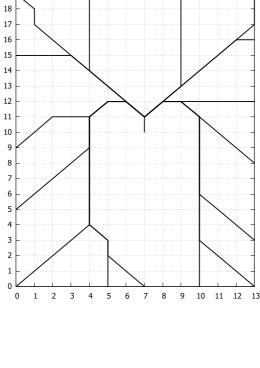
### Experimental Study: Arlanda Airport

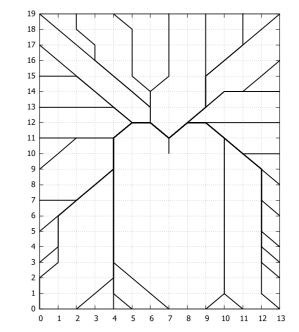


### Increased Number of Entry Points:

#### paths length

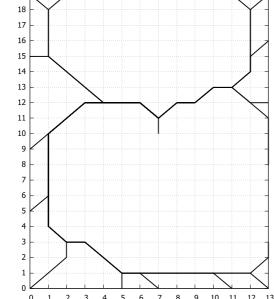


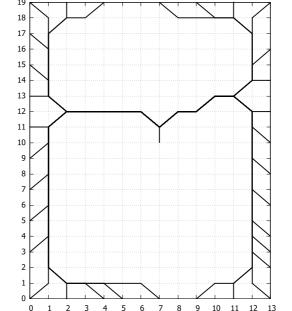




#### 16 entry points

Solutions for large number of entry points could be used to suggest the number and location of entry points for a design from scratch.





2 entry points

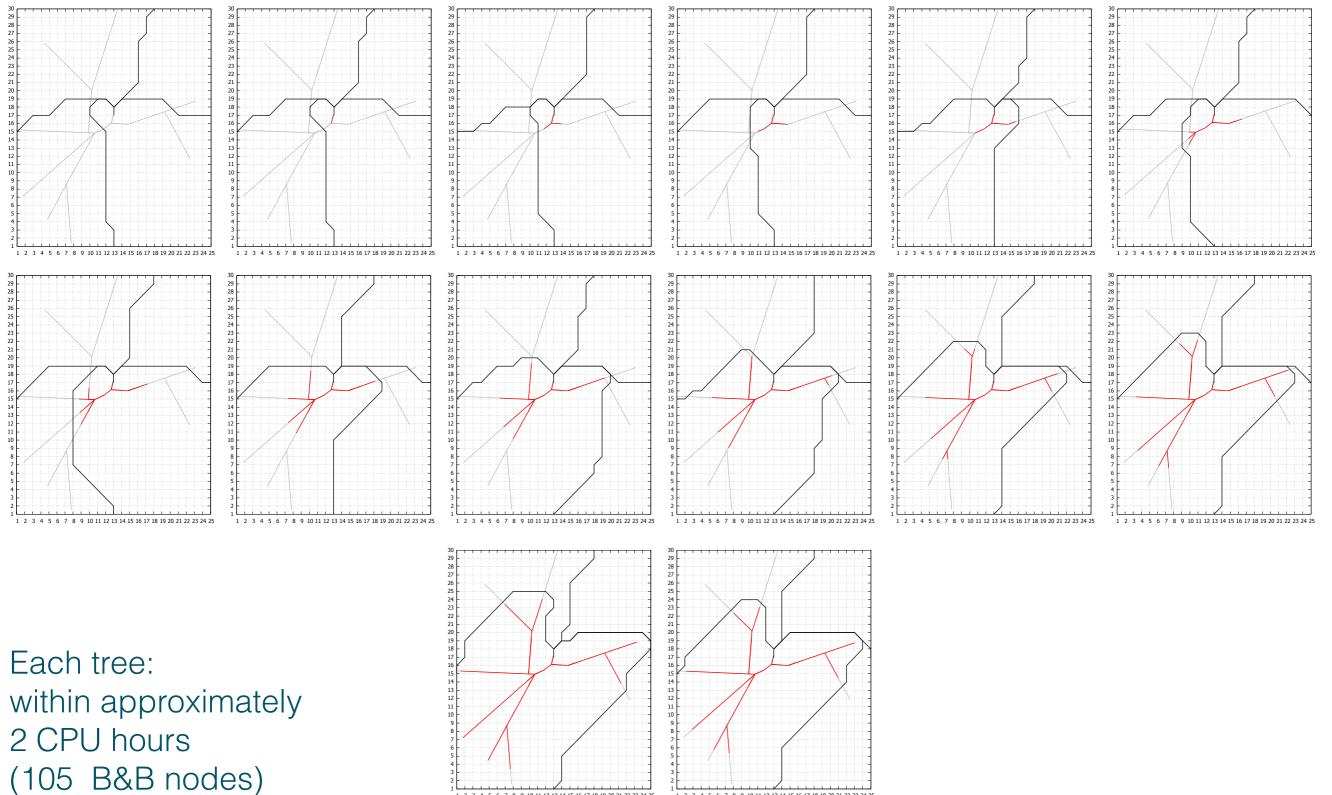
#### Helpful to use linear combination of these two functions

ATMOS, 25.08.2016

Automatic Design of Aircraft Arrival Routes with Limited Turning Angle



### SID constraints:



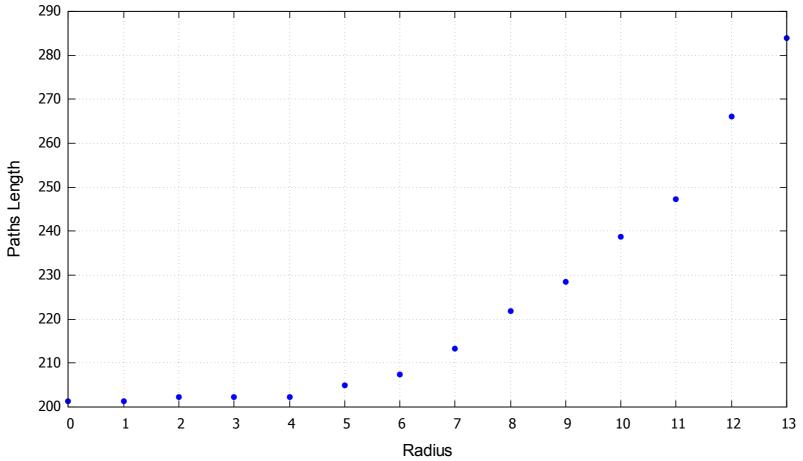
Automatic Design of Aircraft Arrival Routes with Limited Turning Angle

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25

2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25

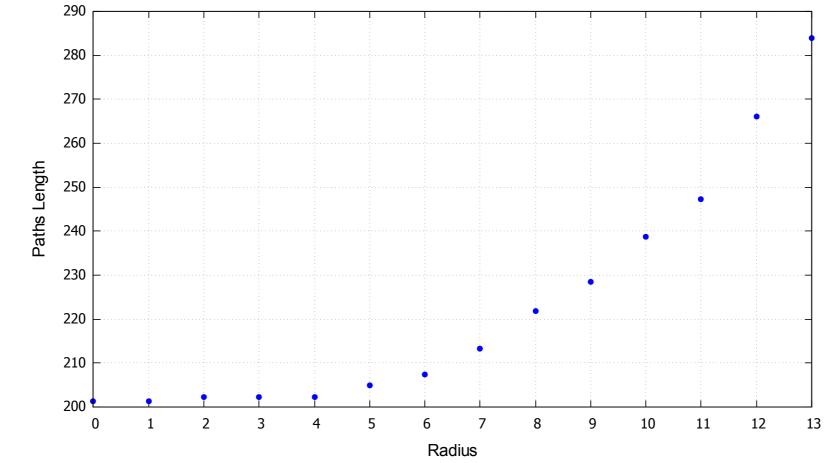


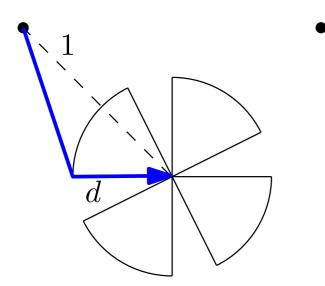
#### SID constraints:



#### LINKÖPING UNIVERSITY

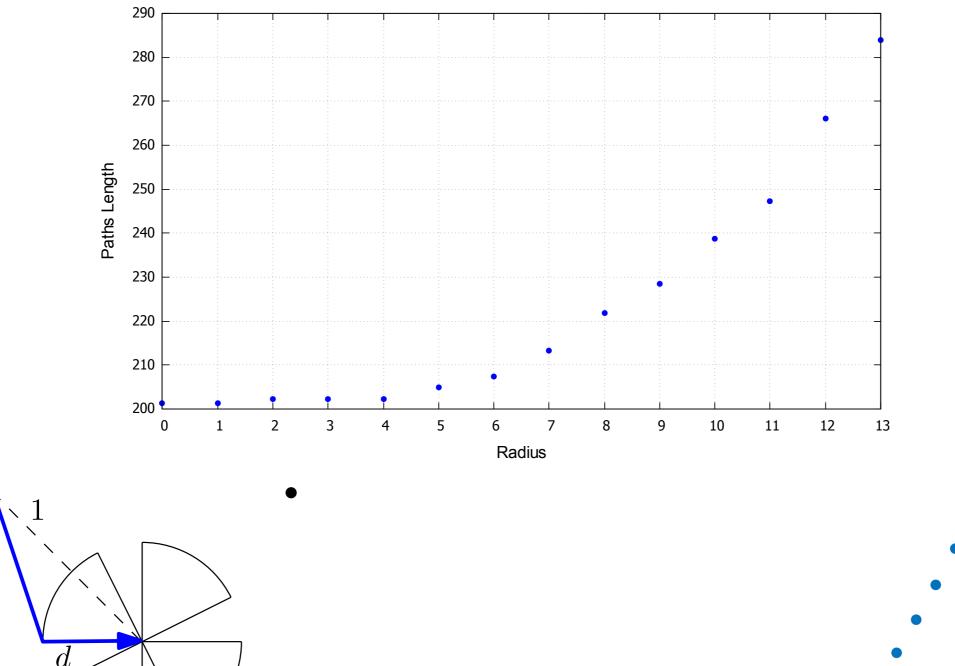
### SID constraints:







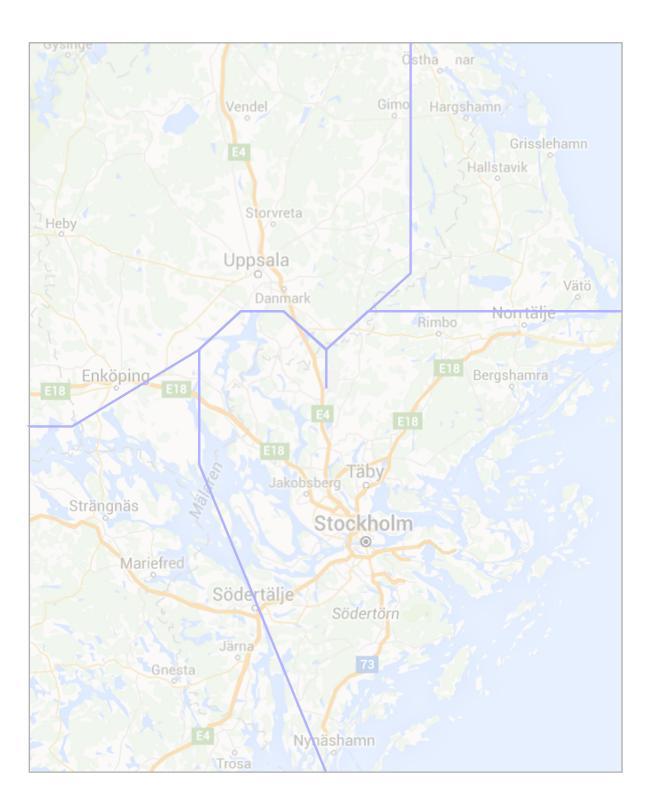
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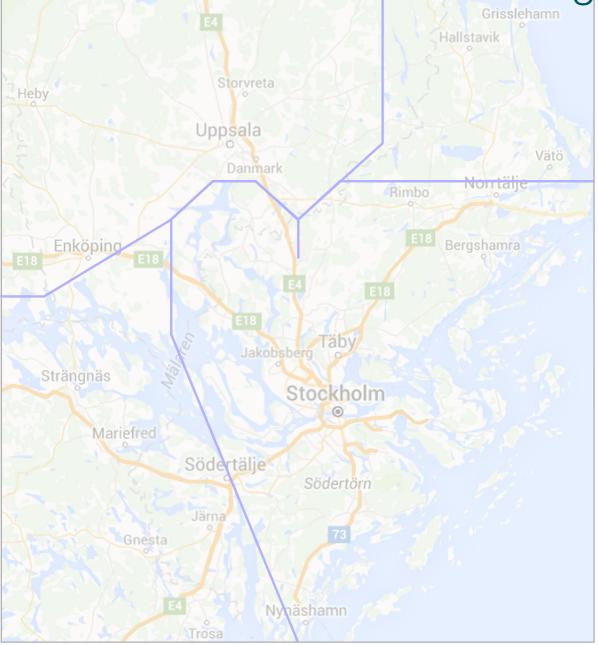


#### Conclusion/Outlook



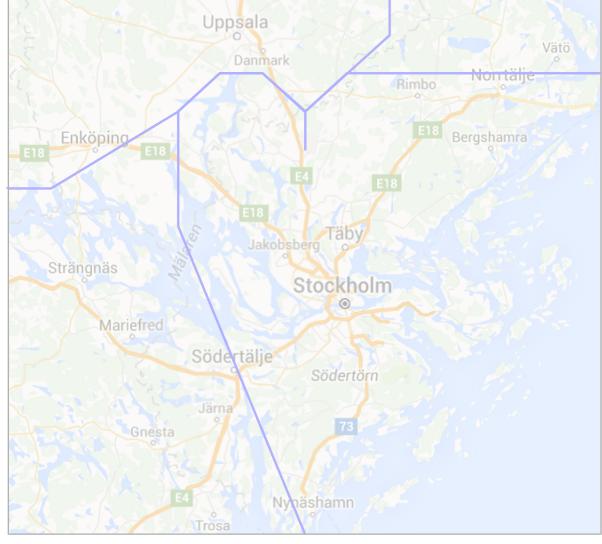




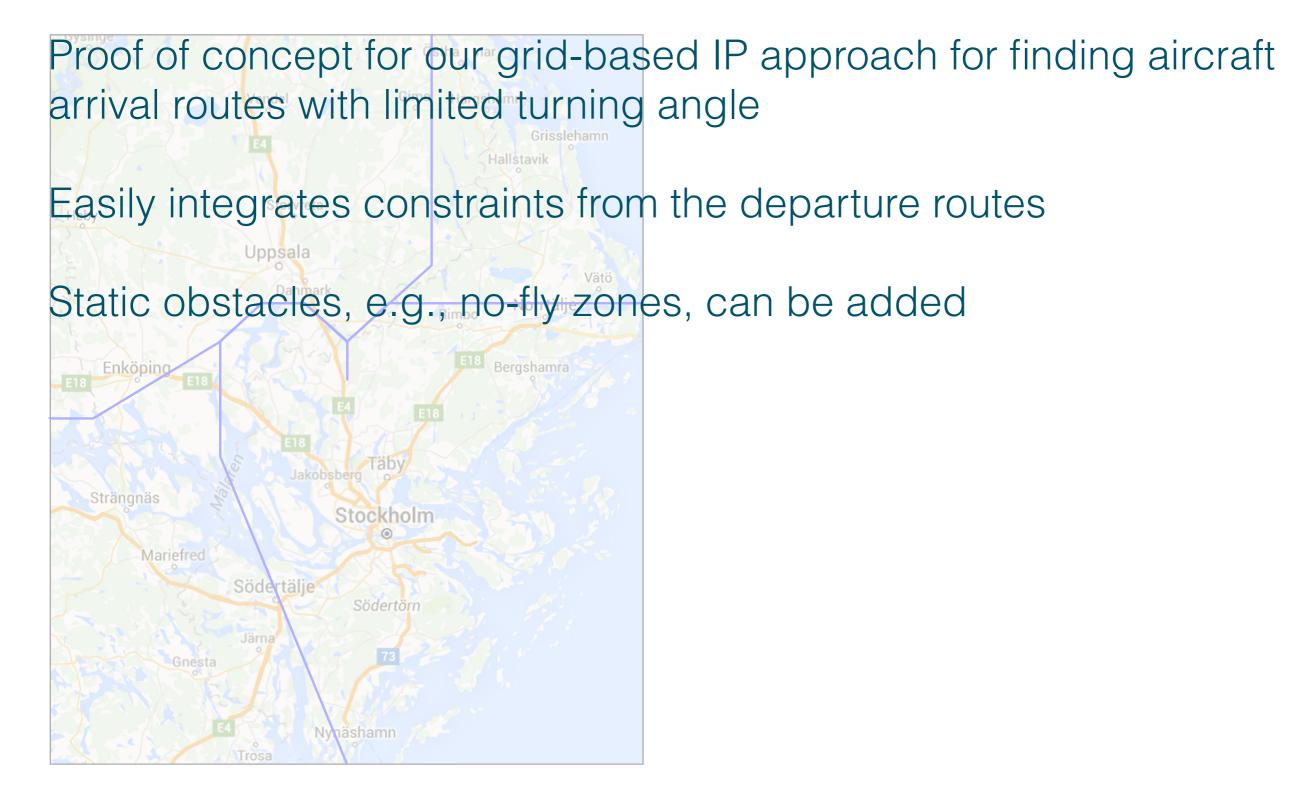




Easily integrates constraints from the departure routes









Easily integrates constraints from the departure routes

Static obstacles, e.g., no-fly zones, can be added

E18 Bergshamra

Might choose to minimize weighted version: minimize the sum of trajectory lengths flown by all arriving aircraft (easily integrated by changing right-hand side of first equation)



Enköning



Easily integrates constraints from the departure routes

Static obstacles, e.g., no-fly zones, can be added

E18 Bergshamra

Might choose to minimize weighted version: minimize the sum of trajectory lengths flown by all arriving aircraft (easily integrated by changing right-hand side of first equation)



Enköping



Easily integrates constraints from the departure routes

Static obstacles, e.g., no-fly zones, can be added

E18 Bergshamra

Uppsala

Might choose to minimize weighted version: minimize the sum of trajectory lengths flown by all arriving aircraft (easily integrated by changing right-hand side of first equation)

Outlook: Södertälje Gnesta Simultaneous design of both SIDs and STARs

Enkönin



Easily integrates constraints from the departure routes

Static obstacles, e.g., no-fly zones, can be added

E18 Bergshamra

Uppsala

Might choose to minimize weighted version: minimize the sum of trajectory lengths flown by all arriving aircraft (easily integrated by changing right-hand side of first equation)

Outlook: Södertälje Gnesta Simultaneous design of both SIDs and STARs 3D routes

Enköping