

# **Confidentiality in Networked Control Systems**

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# **Motivation:** Security of Cyber-Physical Systems (CPS)

- Ubiquitous use of CPS makes them vulnerable to cyber-attacks, due to communication of control inputs and measurements over a network.
- Traditionally, Cyber-attacks are classified by:  $\Delta_{A}$ 
  - Confidentiality, Integrity, Availability.<sup>[1]</sup>
  - Tailored to CPS is the so-called *attacks space*, which is spanned by:
- Model Knowledge, Disclosure, and Disruption Resources.<sup>[2]</sup>
  - We focus on **stealthy actuator attacks**: the attacker wants to stay undetected.
    - $\rightarrow$  Attacker needs to fool the anomaly detector.
    - $\rightarrow$  This requires knowledge of private information within the controller.

**Problem:** Confidentiality attack on the controller

The attacker uses u[k] to estimate the controller states  $x_c[k]$ .

# Estimate $x_c$ by $\hat{x}_c$ perfectly:

# Plant x[k+1] = Ax[k] + Bu[k] + w[k]

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### Attack strategy #1: Kalman filter

First, let  $z[k] = \begin{bmatrix} x[k] \\ x_c[k] \end{bmatrix}$  for the **closed loop state space** formulation.

Due to the noise, this is a random variable. We can set up the Kalman filter as an unbiased estimator:

- 1. Without bias:  $\mathbb{E}[x_c[k] - \hat{x}_c[k]] = \mathbb{E}[e[k]] = 0$
- 2. Zero steady-state error covariance:  $\lim_{k \to \infty} \mathbb{E}[e[k]e[k]^\top] = 0$

y[k] = Cx[k] + v[k] $\uparrow u[k]$  $y[k]\downarrow$ Controller  $x_c[k+1] = A_c x_c[k] + B_c y[k]$  $\boldsymbol{u}[\boldsymbol{k}] = C_c \boldsymbol{x}_c[\boldsymbol{k}] + D_c \boldsymbol{y}[\boldsymbol{k}]$ 

Including independent, zero-mean, Gaussian process and measurement noise  $w[k] \sim \mathcal{N}(0, \Sigma_w)$  and  $v[k] \sim \mathcal{N}(0, \Sigma_v)$ .

**Attack strategy** #2: Unknown Input Observer (UIO)

Describe a series of control signals from a series of measurements:

 $u[k:k+L] = \mathcal{O}_L x_c[k] + \mathcal{J}_L y[k:k+L],$ 

with recursively defined observability  $\mathcal{O}_L$  and invertibility matrix  $\mathcal{J}_L$ :

$$\mathcal{O}_L = \begin{pmatrix} C_c \\ \mathcal{O}_{L-1}A_c \end{pmatrix}; \qquad \qquad \mathcal{J}_L = \begin{pmatrix} D_c & 0 \\ \mathcal{O}_{L-1}B_c & \mathcal{J}_{L-1} \end{pmatrix}.$$

With parameters E and F, the UIO estimates  $x_c[k]$ :

 $\hat{x}_{c}[k+1] = E\hat{x}_{c}[k] + Fu[k:k+L].$ 

In contrast to standard linear Luenberger observer:

- independent of plant outputs y[k: k+L],
- with potential system inherent delay L.

 $z[k+1 \mid \{u[i]\}_{i=0}^k] \sim \mathcal{N}(\hat{z}[k+1], \Sigma_z[k+1]).$ 

For the attacker to estimate  $x_c[k]$  perfectly, we need:

$$\Sigma_z[k] = \mathbb{E}[z[k]z[k]^{\top}], \qquad \lim_{k \to \infty} \Sigma_z[k] = \Sigma_{\infty} = \begin{bmatrix} P & 0 \\ 0 & 0 \end{bmatrix}, \quad P \succeq 0.$$

We can show

1. that  $\Sigma_{\infty}$  is the *unique* and *strong* solution of the filter's Riccati eq. 2. exponential convergence of the covariance towards  $\Sigma_{\infty}$ .

Similarities and Differences		
	#1: Kalman filter	#2: <b>UIO</b>
Estimator	$\hat{z}[k+1] = f_{\mathrm{KF}}(\hat{z}[k], u[k])$	$\begin{split} & \hat{x}_c[k+1] = \\ & f_{\text{UIO}}(\hat{x}_c[k], u[k:k+L]) \end{split}$
Information	controller, plant, noise	only controller
Closed loop	required to be stable	independent from plant
Matrix conditions	$D_c$ full rank and $\rho \big( A_c - B_c D_c^\dagger C_c \big) < 1$	$\begin{split} & \mathrm{rank} \begin{bmatrix} A_c - zI & B_c \\ C_c & D_c \end{bmatrix} = n_c + n_y, \\ & \forall z \in \mathcal{C},  z  \geq 1. \end{split}$
Interpretation	Stable <b>instantaneous</b> right inverse.	Stable <b>L-delay left-</b> <b>inverse</b> / strongly detectable.
$\Rightarrow$ In both	cases: The controller may n	ot have unstable zeros!

#### **Conclusion and Outlook**



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## Sensor attacks (previous work [3]):

Using a **Kalman filter** and plant measurements y[k] for a confidentiality attack, requires the controller to have stable poles.

#### Actuator attacks (our work):

Using a Kalman filter and control inputs u[k] for a confidentiality attack, requires the controller to have stable zeros, and  $D_c$  full rank.

Much less restrictive is the use of an Unknown Input Observer:

- requires less model knowledge and merely strong detectability.
- inherits a potential delay, convergence speed dependent on zeros.

#### **Future work**

Estimate an unknown reference to the controller.



[1]: M. Bishop, E. Sullivan, and M. Ruppel, "Computer security: art and science", [2]: André Teixeira, Iman Shames, Henrik Sandberg, Karl Henrik Johansson, "A secure control framework for resource-limited adversaries", [3]: Umsonst, David; Sandberg, Henrik, "On the confidentiality of controller states under sensor attacks"

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