Uplink Symbol Detection in Dynamic TDD MIMO Systems with AP-AP Interference

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Abstract

We consider a MIMO communication system operating in dynamic TDD, where one uplink (UL) access point (AP) detects data symbols transmitted from UL users (UEs) in the presence of AP-AP interference caused by the signal a downlink (DL) AP transmits to a DL UE. We propose to jointly estimate the UL symbols and the interference channel, but show that this problem is not uniquely solvable in the least-squares sense, and propose two methods for symbol detection that overcome this issue.

System Model



Method 1: Joint Estimation

Disregarding the first sample, the UL AP receives:

$$\overline{\mathbf{Y}} = \mathbf{G}\,\overline{\mathbf{X}} + \mathbf{h}\,\overline{\mathbf{s}}^T + \overline{\mathbf{W}}$$
 or $\overline{\mathbf{y}} = \overline{\mathbf{A}}\overline{\mathbf{z}} + \overline{\mathbf{w}},$

where $\overline{\mathbf{A}}$ is full rank and is obtained by removing the first K columns of A. We propose to jointly estimate the remaining UL data $\overline{\mathbf{X}}$ and h:

$$\min_{\overline{\mathbf{X}},\mathbf{h}} \|\overline{\mathbf{Y}} - \mathbf{G}\,\overline{\mathbf{X}} - \mathbf{h}\,\overline{\mathbf{s}}^T\|^2 \quad \text{or} \quad \min_{\overline{\mathbf{z}}} \|\overline{\mathbf{y}} - \overline{\mathbf{A}}\overline{\mathbf{z}}\|^2,$$

with the unique solution

$$\hat{\bar{\mathbf{z}}} = (\bar{\mathbf{A}}^H \bar{\mathbf{A}})^{-1} \bar{\mathbf{A}}^H \bar{\mathbf{y}}$$

- $\tau_c \in \mathbb{N}$:
- $\mathbf{G} \in \mathbb{C}^{M \times K}$: Channel from UL UEs to UL AP.
- $\mathbf{X} \in \mathbb{C}^{K \times \tau_c}$: Data transmitted from UL UEs.
- $\mathbf{h} \in \mathbb{C}^{M \times 1}$: Effective (single-layer) AP-AP interference channel.
- $\mathbf{s} \in \mathbb{C}^{\tau_c \times 1}$: Data transmitted from DL AP.
- $\mathbf{W} \in \mathbb{C}^{M \times \tau_c}$: Receiver noise at UL AP.

The UL AP receives (on equivalent matrix and vector forms):

 $\mathbf{Y} = \mathbf{G} \, \mathbf{X} + \mathbf{h} \, \mathbf{s}^T + \mathbf{W} \in \mathbb{C}^{M \times \tau_c} \quad \text{or} \quad \mathbf{y} = \mathbf{A} \, \mathbf{z} + \mathbf{w} \in \mathbb{C}^{M \tau_c \times 1}.$

To derive the second expression, recall $\operatorname{vec}(\mathbf{B} \mathbf{C} \mathbf{D}) = (\mathbf{D}^T \otimes \mathbf{B}) \operatorname{vec}(\mathbf{C})$, and define $\mathbf{x} \triangleq \operatorname{vec}(\mathbf{X})$, $\mathbf{y} \triangleq \operatorname{vec}(\mathbf{Y})$, and $\mathbf{w} \triangleq \operatorname{vec}(\mathbf{W})$, to write:

$$\mathbf{y} = (\mathbf{I}_{\tau_c} \otimes \mathbf{G}) \mathbf{x} + (\mathbf{s} \otimes \mathbf{I}_M) \mathbf{h} + \mathbf{w}$$
$$= \underbrace{\left[(\mathbf{I}_{\tau_c} \otimes \mathbf{G}) \quad (\mathbf{s} \otimes \mathbf{I}_M) \right]}_{\triangleq \mathbf{A}} \underbrace{\begin{bmatrix} \mathbf{x} \\ \mathbf{h} \end{bmatrix}}_{\triangleq \mathbf{z}} + \mathbf{w} = \mathbf{A} \mathbf{z} + \mathbf{w}.$$

Problem Formulation

We propose to jointly estimate **X** and **h** with the least-squares method:

$$\min_{\mathbf{X},\mathbf{h}} \|\mathbf{Y} - \mathbf{G}\,\mathbf{X} - \mathbf{h}\,\mathbf{s}^T \|^2 \quad \text{or} \quad \min_{\mathbf{z}} \|\mathbf{y} - \mathbf{A}\,\mathbf{z} \|^2.$$

However, this problem is not uniquely solvable. In fact, the solution space is *K*-dimensional:

Theorem 1. The nullspace of \mathbf{A} is K-dimensional, i.e., so is the solution space to the least-squares problem.

Extract $\hat{\bar{\mathbf{x}}}$ from $\hat{\bar{\mathbf{z}}}$ and reshape to obtain the estimate $\bar{\mathbf{X}}$ of $\bar{\mathbf{X}}$.

Method 2: Interference Subtraction

The first sample is used to obtain the least-squares estimate $\hat{\mathbf{h}}$ of \mathbf{h} :

$$\mathbf{y}_1 = \mathbf{h} \, s_1 + \mathbf{w}_1 \qquad \Rightarrow \qquad \hat{\mathbf{h}} = \frac{s_1^*}{|s_1|^2} \, \mathbf{y}_1$$

Subtract the known part $\hat{\mathbf{h}}\bar{\mathbf{s}}^T$ of the interference before estimating $\overline{\mathbf{X}}$: $\hat{\overline{\mathbf{X}}} = (\mathbf{G}^H \mathbf{G})^{-1} \mathbf{G}^H (\overline{\mathbf{Y}} - \hat{\mathbf{h}} \bar{\mathbf{s}}^T).$

Baseline Algorithms

Define the interference-free signal:

$$\dot{\mathbf{Y}} \triangleq \mathbf{Y} - \mathbf{h} \, \mathbf{s}^T = \mathbf{G} \, \mathbf{X} + \mathbf{W} \quad \text{or} \quad \dot{\mathbf{y}} = \underbrace{(\mathbf{I}_{\tau_c} \otimes \mathbf{G})}_{\triangleq \dot{\mathbf{A}}} \mathbf{x} + \mathbf{w} = \dot{\mathbf{A}} \, \mathbf{x} + \mathbf{w}.$$

We consider one best-case (genie) and one worst-case (naive) baseline:

- Genie (full interference mitigation): $\hat{\overline{\mathbf{X}}} = (\dot{\mathbf{A}}^H \dot{\mathbf{A}})^{-1} \dot{\mathbf{A}}^H \dot{\mathbf{y}}.$
- Naive (no interference mitigation): $\hat{\overline{\mathbf{X}}} = (\dot{\mathbf{A}}^H \dot{\mathbf{A}})^{-1} \dot{\mathbf{A}}^H \mathbf{y}.$

Performance Comparison

Interestingly, our two methods turn out to be equivalent:

Theorem 2. Method 1 and Method 2 are equivalent.

Proof. See [1, Appendix D].

Proof. See [1, Appendix A].

Solution

We solve this by forcing the UL UEs to be silent in their first sample: $\mathbf{X} = [\mathbf{0}_{K \times 1}, \overline{\mathbf{X}}].$

Then, the received signal at the UL AP can be partitioned as $[\mathbf{y}_1, \overline{\mathbf{Y}}] = \mathbf{G}[\mathbf{0}_{K \times 1}, \overline{\mathbf{X}}] + \mathbf{h}[s_1, \overline{\mathbf{s}}^T] + [\mathbf{w}_1, \overline{\mathbf{W}}].$

We propose two methods for symbol estimation:

- Method 1: Joint estimation of data $\overline{\mathbf{X}}$ and interference channel h.
- Method 2: Estimate h with the first sample and subtract interference.

We compare our two methods to the genie and naive baseline algorithms. With $M = 10, K = 3, \tau_c = 50$ and APs/UEs randomly distributed in a $250 \times 250 \text{ m}^2$ square, we get the following bit-error rates (BERs):



